Southwest Windpower Inc.

Doc. # 0185

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27' Air Tower Analysis

7/7/03

1. Introduction:

The following analysis covers tower stress and anchor loads for the Southwest Wndpower 27' Air Tower turbine tower due to wind loading. The tower is built from 1.9" OD schedule 40 steel pipe. The analysis covers the 27 ft tower. The construction of this tower can be seen in fig. 1. Wind drag on the tower is calculated with the use of 1997 UBC standard table. The Air turbine and electrical cable wt. is 10 lb and the thrust load at 100 mph is 80 lb.

The analysis is static only. FEA analysis was used to determine the support point reaction loads and tension in cables. The analysis and results follow.

2. Analysis

Guy wire diameter = .125"Tower bottom section dimension OD = 1.9"Tower top section dimension OD = 1.9"Thrust load from turbine at 100 mph wind speed = 80 lb

The purpose of the analysis is to determine:

- 1. The factor of safety for the most heavily loaded portions of the tower for the given wind speed
- 2. Compliance with the 1997 UBC column loading for given loads.
- 3. The guy cable loads to determine support anchor loads.
- 4. Reaction loads at the tower base (Support requirements)

Quantify loads Wind speed = 100 mph Turbine Thrust = 80 lb

Wind Pressure Ref UBC 1997 section 1613 Exposure D was used as it represents the most severe exposure.

Definitions:

C_e = combined height, exposure and gust factor coefficient

C_a = pressure coefficient for the structure or portion of structure under consideration

- I_{w} = Importance factor
- P = design wind pressure
- q_s = wind stagnation pressure at the standard height of 33 feet

The 1997 UBC design wind pressure equation

$$P = C_e C_q I_w q_s$$

Wind Pressure ref UBC 1997 Exposure D

 $C_e := 1.52$ (taken along full height of tower)

Drag coefficient (C_q) on the tower is found in table 16H UBC 1997 and is equal to:

 $C_q := .8$

Stagnation Pressure (q_s) at 100 mph per table 16F UBC 1997 is equal to:

$$q_s := 25.6 \cdot \frac{\text{lbf}}{\text{ft}^2}$$

Importance factor is found in Table 16K UBC 1997 and is equal to:

$$I_W := 1$$

$$\mathbf{P} := \mathbf{C}_{\mathbf{e}} \cdot \mathbf{C}_{\mathbf{q}} \cdot \mathbf{q}_{\mathbf{s}} \cdot \mathbf{I}_{\mathbf{w}}$$

$$P = 31.13 \frac{lbf}{ft^2}$$

The projected area on the tower is equal to:

$$H_{tower} := 27 \cdot ft$$
 $OD_{pipe} := 1.9 \cdot in$

 $A_{\text{projected}} := H_{\text{tower}} \cdot OD_{\text{pipe}}$

$$A_{\text{projected}} = 4.275 \text{ ft}^2$$

Wind load on the tower is equal to:

 $L_{wind} := A_{projected} \cdot P$

 $L_{wind} = 133.079 \text{ lbf} \qquad L_{ft} \coloneqq \frac{L_{wind}}{27 \cdot \text{ft}} \qquad L_{ft} = 4.929 \frac{\text{lbf}}{\text{ft}}$

The projected area of the guy wire is equal to:

 $F_{guy} = 9.593 \ lbf$ (neglected in analysis)

The cable is connected to the cable hanger by conventional means and looped back onto itself while it is clamped with cable clamps (3 ea. per cable)

The maxium load on the cable is 371 lbf. (axial Loads fig) Typical 1/8" 7X19 Galvanized cable strength = 2000 lbf

Factor of Safety = 5.4 OK

Analyzing the stresses in the guy/coupler extrusion:

Tensile load in the cable: $L_{cable} := 371 \cdot lbf$ (axial loads fig)

Width of tab: $W_{tab} := 1.204 \cdot in$

Thickness of tab: $T_{tab} := .322 \cdot in$

Diameter of cable hole: $D_{hole} := .413 \cdot in$

Cross section area:

$$A_{tab} := W_{tab} \cdot T_{tab} - D_{hole} \cdot T_{tab}$$
 $A_{tab} = 0.255 \text{ in}^2$

Stress in tab:

$$\sigma_{tab} \coloneqq \frac{L_{cable}}{A_{tab}} \qquad \qquad \sigma_{tab} = 1.457 \times 10^3 \text{ psi}$$

Applying stress concentration factor: (fig A-26-1)

ratio :=
$$\frac{D_{hole}}{W_{tab}}$$
 ratio = 0.343

Stress concentration factor = 2.25

$$\sigma_{conc} := 2.25 \sigma_{tab}$$
 $\sigma_{conc} = 3.277 \times 10^3 \text{ psi}$

 $\sigma_{alumyld} \coloneqq 35000 \cdot psi$ (6061-T6)

$$FS_{tab} := \frac{\sigma_{alumyld}}{\sigma_{conc}}$$
 $FS_{tab} = 10.679$ OK

Project____ Project______ Job Number______

Engineer_____

UBC97-LRFD STEEL S Combo : DSTL1 Units : lb, in, F	ECTION CHEC	x									
Frame : 2Design Sect: PIPE1-1/2SCH40X Mid : 0.000Design Type: ColumnY Mid : 12.000Frame Type : Ordinary MRFZ Mid : 288.000Sect Class : SeismicLength : 72.000Major Axis : 0.000 degrees counterclockwise from local 3Loc : 0.000RLLF : 1.000HEQ Factor : 1.000											
Area : 0.799	SMajor : 0.326 AVMajor: 0.448 rMajor : 0						: 0.623				
IMajor : 0.310	SMine	or : 0.326		AVMinor	c: 0.448		rMinor	: 0.623			
IMinor : 0.310	ZMajo	or : 0.448		Ε	: 290000	00.000					
Ixy : 0.000	ZMino	or : 0.448		Fy	: 36000.	000					
STRESS CHECK FORCE	S & MOMENTS										
Location	Pu	Mu33	М	u22	Vu2		Vu3	Tu			
0.000	-36.838	-9533.664	0.	000 -	-152.824	0.	000	0.000			
PMM DEMAND/CAPACI1	Y RATIO	_				_		.			
Governing	Total	P	MMa	jor	MMinor	Ra	tio	Status			
Equation	Ratio	Ratio	. Ra	C10	Ratio	L1 1	mit	Check			
(HI-ID)	0.058	= 0.002	+ 0.	+ / 20	0.000	1.	000	0K.			
AXTAL FORCE DESTGN											
	Pu	phi*Pnc	phi*	Pnt							
	Force	Capacity	Capac	ity							
Axial	-36.838	12099.999	25887.	601							
MOMENT DESIGN					- 0		_	-1			
	Mu	phi*Mn	Cm	B1	B2	_ K	_ L	Cb			
	Moment	Capacity	Factor	Factor	Factor	Factor	Factor	Factor			
Major Moment	-9533.004	14515.200	0.850	1.000	1.000	1.000	1.000	1.729			
MINOr Moment	0.000	14515.200	1.000	1.002	1.000	1.000	1.000				
SHEAR DESIGN											
	Vu	phi*Vn	Str	ess	Status		Tu				
	Force	Capacity	Ratio		Check	Torsion					
Major Shear	152.824	8714.584	0.018		OK	0.000					
Minor Shear	0.000	8714.584	0.000		OK	0.	000				

Project____ Project______ Job Number______

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IMajor : 0.310	SMinor : 0.326 AVMinor: 0.448 rMinor : 0.						: 0.623				
IMinor : 0.310	ZMajo	ZMajor : 0.448 E : 29000000.000									
Ixy : 0.000	ZMino	or : 0.448		Fy	: 36000.	000					
STRESS CHECK FORCE	S & MOMENTS										
Location	Pu	Mu33	Mu	122	Vu2		Vu3	Tu			
0.000	-36.838	-9533.664	0.0	000 -	152.824	0.	000	0.000			
PMM DEMAND/CAPACIT	Y RATIO										
Governing	Total	P	MMai	ior	MMinor	Ra	tio	Status			
Equation	Ratio	Ratio	Ratio		Ratio	Limit		Check			
(H1-1b)	0.658	= 0.002	+ 0.6	557 +	0.000	1.	000	OK			
AXIAL FORCE DESIGN											
	Pu	phi*Pnc	phi*F	nt							
	Force	Capacity	Capaci	ty							
Axial	-36.838	12099.999	25887.6	501							
MOMENT DESTGN											
	Ми	phi*Mn	Cm	в1	в2	к	L	Cb			
	Moment	Capacity	Factor	Factor	Factor	Factor	Factor	Factor			
Major Moment	-9533.664	14515.200	0.850	1.000	1.000	1.000	1.000	1.729			
Minor Moment	0.000	14515.200	1.000	1.002	1.000	1.000	1.000				
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Major Shear	152.824	8714.584	0.018		OK	0.000					
Minor Shear	0.000	8714.584	0.000		OK	0.	000				

TOWER CABLE ANCHOR DESIGN

DESCRIPTION:

Concrete anchor for the Southwest Windpower Air 27' and 45' Tower Models. Supporting cables from the tower are attached to the concrete anchor via and eye bolt and cable clamp arrangement.

LOADS:

Per Restrains Reactions fig., the maxium anchor loads are due to wind loading. They are 494 lbf in the vertical up direction and 359 lbf in the horizontal direction.

SOILS INFORMATION: NA

It is assumed the anchor will be located in sandy soil. The recommended UBC guidelines

for allowable soil bearing capacity are used to determine adequacy of the anchor to

support the loads. It is assumed that all fill is compacted.

Bearing strength is taken as 1500 PSF Lateral bearing strength is taken s 150 PSF/ (ft depth) Friction is taken as .25 X effective anchor weight.

ANCHOR WEIGHT:

Reference drawing R00003 for dimensions.

CONCRETE VOLUME:

 $Concrete_{weight} = 436.4 \, \text{lbf}$

OVER BURDEN VOLUME:

Height := 16·in

$$V_{ob} := (\pi \cdot Base_{radius}^{2} \cdot Height) - Column_{width}^{2} \cdot Height$$

$$V_{ob} = 3.6 \text{ ft}^{3}$$
Density_{ob} := 75 $\cdot \frac{\text{lbf}}{\text{ft}^{3}}$
Weight_overburden := $V_{ob} \cdot Density_{ob}$ Weight_overburden = 269.7 lbf
Total_weight := Concrete_weight + Weight_overburden
Total_weight = 706.1 lbf O.K.
Anchor_bearing := $\pi \cdot Base_{radius}^{2}$ Anchor_bearing = 3.1 ft^{2}
Soil_pressure := $\frac{\text{Total}_{weight}}{\text{Anchor}_{bearing}}$
Soil_pressure = $224.8 \frac{\text{lbf}}{\text{ft}^{2}}$ OK

LATERAL RESISTANCE:

Total_{lateral} := Lateral_{resisting} + Lateral_{friction}

 $Total_{lateral} = 586.4 \, lbf$ O.K.

REINFORCING STEEL:

 $\begin{aligned} \mathsf{F}_{\text{vertical}} &= 494 \, \text{lbf} & \mathsf{F}_{\text{horizontal}} \coloneqq 359 \cdot \text{lbf} & \text{Column}_{\text{width}} \coloneqq 8 \cdot \text{in} \\ \tau_{\text{max}} &\coloneqq \frac{\mathsf{F}_{\text{horizontal}}}{\mathsf{Column}_{\text{width}}^2} & \tau_{\text{max}} = 5.6 \, \text{psi} & \mathsf{OK} \end{aligned}$ $\sigma_{\text{max}} &\coloneqq \frac{\mathsf{F}_{\text{vertical}}}{\mathsf{Column}_{\text{width}}^2} & \sigma_{\text{max}} = 7.7 \, \text{psi} & \mathsf{OK} \end{aligned}$

Minimum Reinforcement required:

Per UBC sec 1910.5.3 reinforcing steel area is to be 1.33 times greater than that required by analysis.

Load at the 8"x8" section = 494 lbf axial tension + maximum possible transfer moment to the base of that section = 359 lbf X 22" = 658.2 lbf*ft.

Tensile load in the Rebar:

 $M_r := 658.2 \cdot lbf \cdot ft$ width_{center} := 4 · in

 $Tensile_{rebar} := \frac{M_r}{width_{center}} + F_{vertical}$ Tensile_{rebar} = 2468.6 lbf

Per UBC section 1909.2.2, tensile load:

 $T_{UBC} := 1.33 \cdot Tensile_{rebar}$ $T_{UBC} = 3283.2 \, lbf$

Required Rebar Area:

 $A_{rebar} := \frac{T_{UBC}}{40000 \cdot psi} \qquad A_{rebar} = 0.1 \text{ in}^2$ #4 rebar= .196 \cdot in² OK Use one strand #4 centered in column section for base to column connection. Use two strands #4 in each direction perpendicular to each other in base as shown in drawing R00003. Per UBC table 19D use 1/2" Eyebolt embedded into concrete 6" deep tied adjacent to rebar.



Conclusion:

This analysis is a maximum load condition static analysis only; no fatigue analysis is contained herein. This analysis pertains to the 27 ft "Air" Turbine tower with construction and loading as described in appendix A, and does not address the operation of the turbine or the connection of the turbine to the tower. Loading conditions are at 100 mph. Proper assembly is assumed.

The sections of the tower were checked to see that it meets UBC requirements against buckling which it does. This requirement is the limiting factor for wind speed for the tower.

Guy wire stress is maximum in the top guy wire.

Appendix A

















FIGURE A-26-1 Bar in tension or simple compression with a transverse hole. $\sigma_0 = F/A$, where A = (w - d)t, and where t is the thickness.



FIGURE A-26-2 Rectangular bar with a transverse hole in bending. $\sigma_0 = Mc/I$, where $I = (w - d)h^3/12$.

^{*} Unless otherwise stated, these factors are from R. E. Peterson, "Design Factors for Stress Concentration," *Machine Design*, vol. 23, no. 2, February 1951, p. 169, no. 3, March 1951 p.161; no. 5, May 1951, p. 159; no. 6, June 1951, p. 173; no. 7, July 1951, p. 155; reproduced with the permission of the author and publisher.